2. 式の乗法, 除法② (システム P6~7)

$(a+b)(c+d)$ の計算

最初に, $c+d$ の部分を別の文字 A に置き換えてみると

$$\begin{aligned}
 (a+b)(c+d) &= (a+b)A && \text{前回の分配法則を使って}\dots \\
 &= aA + bA && A \text{の部分をもとの式に戻すと}\dots \\
 &= a(c+d) + b(c+d) && \text{もう一度 分配法則で}\dots \\
 &= ac + ad + bc + bd
 \end{aligned}$$

結果的に, ①~④を順番にかけあわせていくと計算できます。

$$(a+b)(c+d) = \overset{\textcircled{1}}{a} \overset{\textcircled{2}}{c} + \overset{\textcircled{1}}{a} \overset{\textcircled{2}}{d} + \overset{\textcircled{3}}{b} \overset{\textcircled{2}}{c} + \overset{\textcircled{3}}{b} \overset{\textcircled{2}}{d}$$

多項式の () を外して, いくつかの積の形に表すこと → 展開

$$(x-3)(y+5) = \overset{\textcircled{1}}{x} \overset{\textcircled{2}}{y} + \overset{\textcircled{1}}{x} \overset{\textcircled{2}}{5} - \overset{\textcircled{3}}{3} \overset{\textcircled{2}}{y} - \overset{\textcircled{3}}{3} \overset{\textcircled{2}}{5}$$

$$(2a+3)(3b-1) = 6ab - 2a + 9b - 3$$

※ 展開したときに同類項があれば, まとめて答えます。

$$\begin{aligned}
 (x-4)(x-7) &= \overset{\textcircled{1}}{x} \overset{\textcircled{2}}{x} - \overset{\textcircled{1}}{x} \overset{\textcircled{2}}{7} - \overset{\textcircled{3}}{4} \overset{\textcircled{2}}{x} + \overset{\textcircled{3}}{4} \overset{\textcircled{2}}{7} \\
 &= x^2 - 11x + 28
 \end{aligned}$$

$$\begin{aligned}
 (3a+2b)(2a-b) &= \overset{\textcircled{1}}{3a} \overset{\textcircled{2}}{2a} - \overset{\textcircled{1}}{3a} \overset{\textcircled{2}}{b} + \overset{\textcircled{3}}{2b} \overset{\textcircled{2}}{2a} - \overset{\textcircled{3}}{2b} \overset{\textcircled{2}}{b} \\
 &= 6a^2 + ab - 2b^2
 \end{aligned}$$